

# Mathematics (Economics, Markets and Finance)

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## Homework 1

**Exercise 1.** Find the natural domain of the following functions.

a)  $f_1(x) = \sqrt{x^2 - 6x + 10}.$

b)  $f_2(x) = \sqrt{4x^2 - 4x + 1}.$

c)  $f_3(x) = \frac{1}{\sqrt{x-1}}.$

d)  $f_4(x) = \frac{x+2}{x^2 - 3x + 2}.$

e)  $f_5(x) = e^{1/(x-1)}.$

f)  $f_6(x) = \ln \sqrt{x+3}.$

g)  $f_7(x) = \ln \frac{1}{\sqrt{x-3}}.$

h)  $f_8(x) = \sqrt[3]{\frac{x}{x^2 - 1}}.$

i)  $f_9(x) = \sqrt{x} + \sqrt{x-1}.$

j)  $f_{10}(x) = e^{\sqrt{x+2}}.$

k)  $f_{11}(x) = \ln(e^x + 2).$

l)  $f_{12}(x) = \sqrt{x^2 + e^{x+3}}.$

m)  $f_{13}(x) = \ln(x+1) + e^{1/x}.$

n)  $f_{14}(x) = \ln(x+1) - 3 \ln(x+2).$

o)  $f_{15}(x) = \sqrt{x-1} + \ln x - 1.$

p)  $f_{16}(x) = \sqrt{\frac{x-1}{x-2}}.$

**Exercise 2.** Given the function

$$f(x) = \begin{cases} e^{-x}, & \text{if } x \leq 0; \\ x + 1, & \text{if } x > 0; \end{cases},$$

plot its graph and determine whether it is continuous or not.

**Exercise 3.** Given the function

$$f(x) = \begin{cases} e^{-ax} + a, & \text{if } x \leq 0; \\ -x + 2, & \text{if } x > 0; \end{cases},$$

where  $a \in \mathbb{R}$  is a parameter, find the value of  $a$  that makes  $f$  continuous. Plot the graph of  $f$  with this value of  $a$ .

**Exercise 4.** Given the function

$$f(x) = \begin{cases} 2x + a, & \text{if } x \leq 1; \\ x^2 + 3, & \text{if } x > 1; \end{cases},$$

where  $a \in \mathbb{R}$  is a parameter, find the value of  $a$  that makes  $f$  continuous. Plot the graph of  $f$  with this value of  $a$ .

**Exercise 5.** Given the function

$$f(x) = \begin{cases} e^{2x+a}, & \text{if } x \geq 0; \\ x + 2, & \text{if } x < 0; \end{cases},$$

where  $a \in \mathbb{R}$  is a parameter, find the value of  $a$  that makes  $f$  continuous.

**Exercise 6.** Given the function

$$f(x) = \begin{cases} ae^{3x}, & \text{if } x \geq -1; \\ x^8 + bx + 1, & \text{if } x < -1; \end{cases},$$

where  $a, b \in \mathbb{R}$  are parameters, find all the values of  $a$  and  $b$  that make  $f$  continuous.

**Exercise 7.** Plot the graph of the function

$$f(x) = \begin{cases} e^x, & \text{if } x < 0; \\ 2, & \text{if } 0 < x \leq 1; \\ x^2 + 1, & \text{if } x > 1. \end{cases}$$

Using the graph find whether  $f$  is continuous.