

*Corso di Matematica e Statistica - Esercizi proposti - Gruppo 1*

**Calcolare i limiti seguenti**

1.  $\lim_{x \rightarrow +\infty} 1 - 2x + x^2 - x^3$

2.  $\lim_{x \rightarrow -\infty} \frac{x^4 - 2x^2 + x}{3x^4 + 2x - 1}$

3.  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2}$

4.  $\lim_{x \rightarrow -1} \frac{x^3 - 1}{x - 1}$

5.  $\lim_{x \rightarrow 0} \frac{\sin^2 x}{x}$

6.  $\lim_{x \rightarrow 0^+} \frac{\sin^2 x}{x^3}$

7.  $\lim_{x \rightarrow 0^-} \frac{\sin^2 x}{x^3}$

8.  $\lim_{x \rightarrow 0} \frac{\sin^2 x}{x^4}$

9.  $\lim_{x \rightarrow 0} \frac{\sin 2x}{3x}$

10.  $\lim_{x \rightarrow -\infty} \frac{x^2 - 2x + 1}{5x^3 + x + 2}$

11.  $\lim_{x \rightarrow +\infty} \frac{1}{x - x^2}$

12.  $\lim_{x \rightarrow +\infty} \frac{\sin x}{x}$

**Calcolare le derivate delle seguenti funzioni**

1.  $f(x) = (x + 2)^{12}$

2.  $f(x) = \frac{x - 1}{x^2 + 1}$

3.  $f(x) = x^2 \sin x + \frac{1}{x^3}$

4.  $f(x) = \sqrt{x} + \sqrt[5]{x}$

5.  $f(x) = \frac{\sqrt{x} + 1}{x^2 - 1}$

6.  $f(x) = e^{x^2+1}$

7.  $f(x) = \ln(\cos(2x + 3))$

8.  $f(x) = x^2 \sin x \ln x$